

Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

7511236721

CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/42

Paper 4 (Extended)

October/November 2015

2 hours 15 minutes

Candidates answer on the Question Paper.

Additional Materials: Geometrical Instruments

Graphics Calculator

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

Do not use staples, paper clips, glue or correction fluid.

You may use an HB pencil for any diagrams or graphs.

DO NOT WRITE IN ANY BARCODES.

Answer all the questions.

 $\hbox{Unless instructed otherwise, give your answers exactly or correct to three significant figures as appropriate. }$

Answer in degrees should be given to one decimal place.

For π , use your calculator value.

You must show all the relevant working to gain full marks and you will be given marks for correct methods, including sketches, even if your answer is incorrect.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 120.

This document consists of 20 printed pages.



Formula List

For the equation

$$ax^2 + bx + c = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Curved surface area, A, of cylinder of radius r, height h.

$$A = 2\pi rh$$

Curved surface area, A, of cone of radius r, sloping edge l.

$$A = \pi r l$$

Curved surface area, A, of sphere of radius r.

$$A = 4\pi r^2$$

Volume, V, of pyramid, base area A, height h.

$$V = \frac{1}{3}Ah$$

Volume, V, of cylinder of radius r, height h.

$$V = \pi r^2 h$$

Volume, V, of cone of radius r, height h.

$$V = \frac{1}{3}\pi r^2 h$$

Volume, V, of sphere of radius r.

$$V = \frac{4}{3}\pi r^3$$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$Area = \frac{1}{2}bc \sin A$$

Answer all the questions.

1 (a) By writing each number correct to 1 significant figure, find an estimate for

$$\frac{\sqrt[3]{987}}{5.13} + \frac{(16.3 + 1.91^2)}{\sqrt{9.12}}.$$

You must show your working.

	Answer(a)[2
(b)	Explain why your answer to part (a) is greater than the actual answer.
	Answer(b)
	[2
(c)	Work out.
	$\frac{\sqrt[3]{987}}{5.13} + \frac{(16.3 + 1.91^2)}{\sqrt{9.12}}.$

Answer(c)[1]

2	(a)	Solve th	e equation	ne
4	(a)	Soive u	ie equalic	ms.

(i)
$$4\log 3 - 3\log 4 = \log x - 5\log 2$$

$$Answer(a)(i) x = \dots [3]$$

(ii)
$$4\sin x + 3 = 1$$
 for $0^{\circ} \le x \le 360^{\circ}$

(b) Make x the subject of the formula.

$$a = \sqrt{\frac{x-1}{x}}$$

$$Answer(b) x = \dots [3]$$

3 The table gives the marks of 10 students in a geography exam and a history exam.

Geography mark (x)	12	23	36	41	57	62	78	81	89	93
History mark (y)	32	43	41	51	52	60	68	65	76	80

(a)	Fin	d
\ · · · /	1 111	u

(i) the mean geography mark,

Answer(*a*)(i)[1]

(ii) the mean history mark.

(b) (i) Find the equation of the regression line for y in terms of x.

 $Answer(b)(i) y = \dots [2]$

(ii) Estimate the history mark when the geography mark is 51.

Answer(*b*)(ii)[1]

The transformation P is a reflection in the *x*-axis.

4

	(i)	the inverse of P,	
		Answer(a)(i)	
((ii)	the inverse of Q.	
		Answer(a)(ii)	•••••
		Answer(a)(ii)	
o)]	Des		
		scribe fully the single transformation equivalent to P followed by Q.	
	Ans	scribe fully the single transformation equivalent to P followed by Q. Swer(b)	
	Ans	scribe fully the single transformation equivalent to P followed by Q.	
	Ans	scribe fully the single transformation equivalent to P followed by Q. Swer(b)	
	Ans	scribe fully the single transformation equivalent to P followed by Q. Swer(b)	
	Ans	scribe fully the single transformation equivalent to P followed by Q. Swer(b)	

Find the next term and the nth term in each of the following sequences.

(a) 27, 20, 13, 6, -1,	
	Answer(a) next term =
a) 1001 - 510 - 056 - 100	nth term =[3]
(b) 1024, 512, 256, 128,	64,
	Answer(b) next term =
	<i>n</i> th term =[3]

5

6 The marks, *x*, of 800 students in a mathematics exam are given in the table.

Mark (x)	Frequency
$0 < x \le 20$	62
$20 < x \le 30$	84
$30 < x \le 40$	140
$40 < x \le 50$	160
$50 < x \le 60$	142
$60 < x \le 80$	112
$80 < x \le 100$	100

(a) Calculate an estimate of the mean mark.

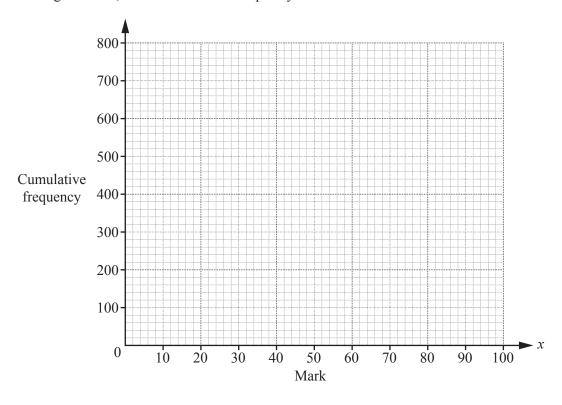
Answer(a)		2	1	
-----------	--	---	---	--

(b) Complete the cumulative frequency table.

Mark (x)	Cumulative frequency
$0 < x \le 20$	62
$0 < x \le 30$	
$0 < x \le 40$	
$0 < x \le 50$	
$0 < x \le 60$	
$0 < x \le 80$	
$0 < x \le 100$	800

[1]

(c) On the grid below, draw a cumulative frequency curve.



(d) Use your graph in part (c) to find estimates for

(i) the median mark,

Answer(d)(i)......[1]

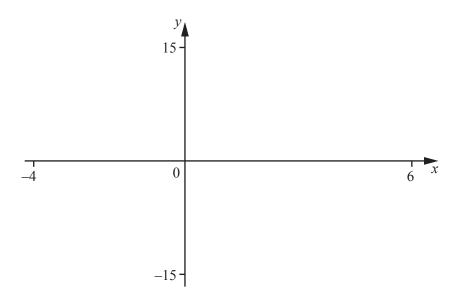
[3]

(ii) the interquartile range,

Answer(d)(ii)[2]

(iii) the minimum mark for a candidate to obtain a grade A, given that 15% of students gain a grade A.

7



$$f(x) = \frac{(6x+11)}{(2x-3)}$$

- (a) (i) On the diagram, sketch the graph of y = f(x), for values of x between x = -4 and x = 6. [2]
 - (ii) Write down the equations of the asymptotes.

(iii) Write down the co-ordinates of the points where the graph crosses the axes.

(b) Solve the inequality.

$$x < \frac{(6x+11)}{(2x-3)}$$

Answer(b).....[4]

	do lives in Manchester. He drives to Cambridge for a meeting. distance from Manchester to Cambridge is 300 km.
(a)	Freddo leaves Manchester at 0705 and arrives in Cambridge at 1050.
	Calculate his average speed.
	Answer(a)
(b)	After the meeting Freddo drives back to Manchester. His average speed for this journey is 5% more than his average speed driving to Cambridge. He leaves Cambridge at 1745.
	Find the time Freddo arrives in Manchester.
	Answer(b)[3]
(c)	Freddo's car uses fuel at the rate of 8.1 km per litre. Fuel costs £1.45 per litre.
	Find the total cost of fuel for Freddo's journey from Manchester to Cambridge and back to Manchester.
	$Answer(c) £ \qquad [2]$

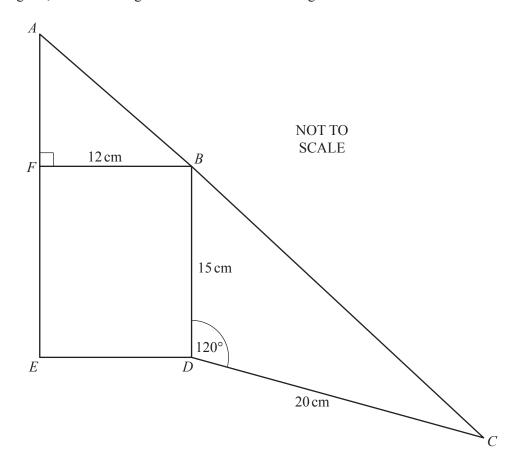
9	(a)	A coat costs \$100. The price is increased by 10% and then decreased by 10%.
		Find the new price of the coat.
		<i>Answer(a)</i> \$[2]
	(b)	A chair costs \$1000. The price is increased by 20% and then decreased by 20%.
		Find the new price of the chair.
		<i>Answer(b)</i> \$[2]
	(c)	A car costs \$10 000.
		The price is increased by $x\%$ and then decreased by $x\%$.
		Find an expression, in terms of <i>x</i> , for the new price of the car. Give your answer in its simplest form.
		Ancupar(a) \$

10	A bag contains 3 red balls and 5 blue balls. In an experiment, three balls are chosen at random without replacement.					
	(a)	Find the probability that the three balls chosen are				
		(i)	all red,			
				Answer(a)(i)	[2]	
		(ii)	two red and one blue,			
				Answer(a)(ii)	[3]	
		(iii)	at least one of each colour.			
				Answer(a)(iii)	[3]	
	<i>a</i>)	ari .				
	(b)		s experiment is to be carried out 1680			
		Fin	d the expected frequency of 3 red ball	s being chosen.		
				Answer(b)	[2]	
				2216 1101 (0)		

11	A is	the point $(2, 6)$ and C is the	point (5, 4).				
	The The	equation of the line AB is equation of the line BC is	y + 4x = 14. $y = x - 1.$				
	(a)	B is the point where the lines AB and BC intersect.					
		Find the co-ordinates of the point <i>B</i> .					
				Answer(a) (,) [3]
	(b)	M is the midpoint of AC .					,
		Find the co-ordinates of M	ſ.				
				Answer(b) (,) [2]

(c)	Find the equation of the line <i>BM</i> .		
		Answer(c)	[3
(d)	The point D lies on the line BM . The co-ordinates of D are $(k, k+9)$.		
	Find the value of k .		
		$Answer(d) k = \dots$	[2]

12 In the diagram, ABC is a straight line and BFED is a rectangle.



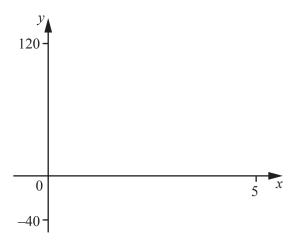
(a) Find BC.

(b) Show that angle $DBC = 34.7^{\circ}$, correct to 3 significant figures.

[3]

(c)	Find the perimeter of the quadrilateral ACDE.	
		Answer(c)
(d)	Find the area of the quadrilateral <i>ACDE</i> .	
		Answer(d) cm^2 [3]

13



$$f(x) = \frac{100}{2^x} - 10$$

- (a) (i) On the diagram, sketch the graph of y = f(x), for $0 \le x \le 5$. [2]
 - (ii) Write down the x co-ordinate of the point where the graph crosses the x-axis.

(iii) Write down the range of f(x).

(b) Solve the equation.

$$\frac{100}{2^x} - 10 = 20$$

$$Answer(b) x = \dots [1]$$

(c) Describe fully the **single** transformation that maps the graph of $y = \frac{100}{2^x}$ onto the graph of $y = \frac{100}{2^x} - 10$.

14		A fraction P has denominator x . The numerator of the fraction is 3 less than the denominator.				
	(a)	Write down fraction P in terms of x .				
		Answer(a)	[1]			
	(b)	The numerator and the denominator of fraction P are each increased by 3 to give fraction Q .				
		Write down fraction Q in terms of x .				
		Answer(b)	[1]			
	(c)	$Q - P = \frac{9}{40}$				
		(i) Write down an equation in x and show that it simplifies to $x^2 + 3x - 40 = 0$.				
			[3]			
		(ii) Solve the equation $x^2 + 3x - 40 = 0$.				
		$Answer(c)(ii) x = \dots or x = \dots$	[2]			
		(iii) Write down the original fraction, P .				
		Answer(c)(iii)	[1]			

Question 15 is printed on the next page.

15 Solve the inequalities.

(a)
$$\frac{5}{2x-1} < 3$$

(b) $\log(2^x) > 10$

Answer(b)[2]

Permission to reproduce items where third-party owned material protected by copyright is included has been sought and cleared where possible. Every reasonable effort has been made by the publisher (UCLES) to trace copyright holders, but if any items requiring clearance have unwittingly been included, the publisher will be pleased to make amends at the earliest possible opportunity.

To avoid the issue of disclosure of answer-related information to candidates, all copyright acknowledgements are reproduced online in the Cambridge International Examinations Copyright Acknowledgements Booklet. This is produced for each series of examinations and is freely available to download at www.cie.org.uk after the live examination series.

Cambridge International Examinations is part of the Cambridge Assessment Group. Cambridge Assessment is the brand name of University of Cambridge Local Examinations Syndicate (UCLES), which is itself a department of the University of Cambridge.